

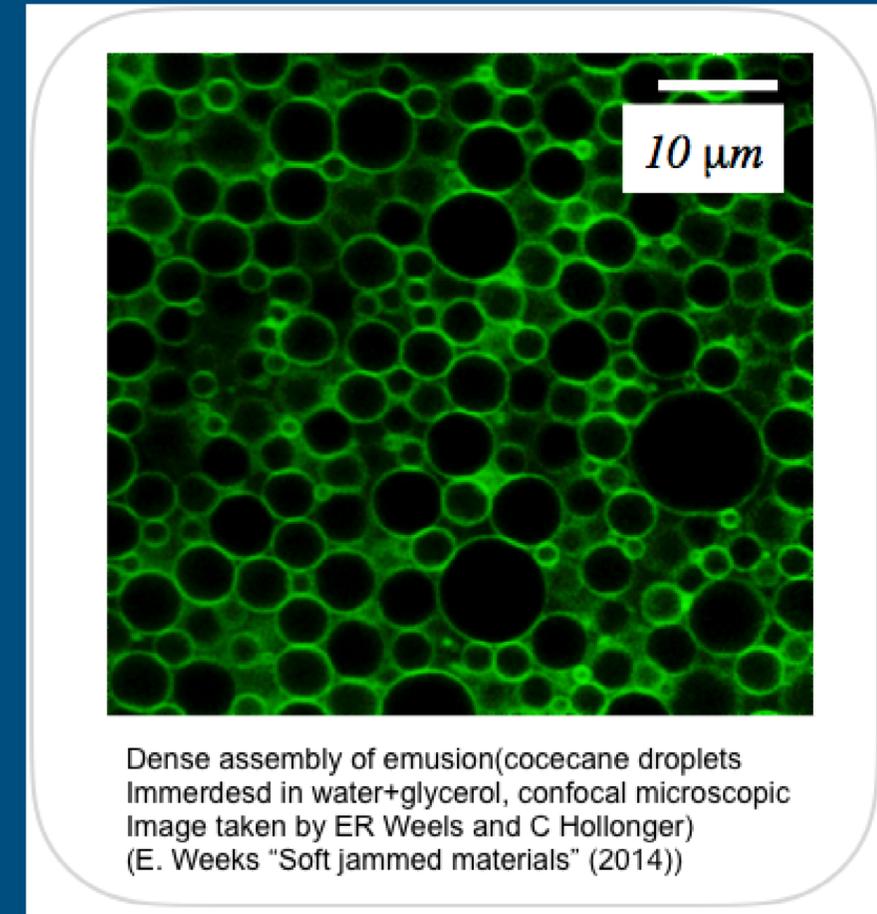
State following of amorphous soft-condensed matters:
developments of high-performance computational schemes

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■ Purpose of the project



The purpose of this project is to develop a set of high-performance computational schemes to study rheological properties of amorphous solid states of soft-matter such as dense assemblies of colloids and emulsions (see the right figure). Our project is motivated by the recent developments of the mean-field theory for amorphous, glassy soft-matters in recent years [1] which produced interesting predictions on the rheological properties [2, 3, 4]. However the mean-field theory is exact only in the large dimensional limit and its validity in the real three dimensional systems is a totally open question

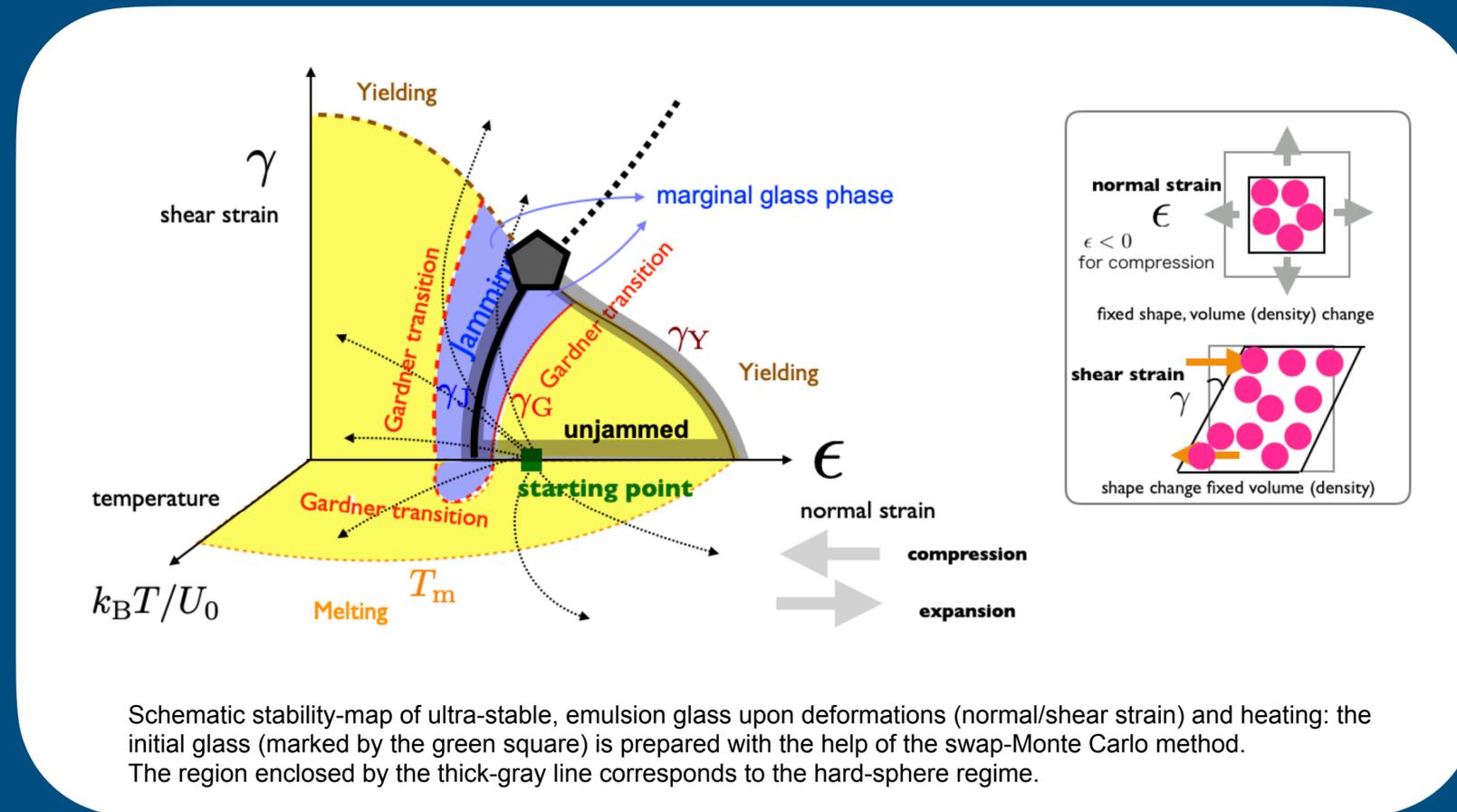
[1] Patrick Charbonneau, Jorge Kurchan, Giorgio Parisi, Pierfrancesco Urbani, and Francesco Zamponi. Nature communications, 5:3725, 2014.

[2] Hajime Yoshino and Francesco Zamponi. Physical Review E, 90(2):022302, 2014.

[3] Corrado Rainone, Pierfrancesco Urbani, Hajime Yoshino and Francesco Zamponi, Phys. Rev. Lett. 114(1), 015701, 2015

[4] Pierfrancesco Urbani and Francesco Zamponi. Phys. Rev. Lett. , 118(3), 038001, 2017.

Development of parallelized rheology simulation schemes



1. Preparation of ultra-stable glassy states at low temperatures/high densities. Such a state is represented as the 'starting point' - the green-square point - in the figure. This is a hard-sphere configuration in a glassy state.
2. Glass state following under quasi-static perturbations As shown in the figure, we explore the system under perturbations by applying the volume strain ϵ , shear-strain γ and temperature T . (k_B is the Boltzmann's constant.) Here U_0 is the energy scale for the deformation of spheres so that $U_0 \rightarrow \infty$ in the hard-spheres. With the hard-spheres, we are confined in the $k_B T / U_0 = 0$ plane. Starting from the initial configuration (green-square), we can bring the assembly of hard-spheres to each point in the region bounded by the thick-gray line. The hard-sphere glass state yields beyond the yielding line γ_Y and jams approaching shear-jamming line γ_J .

■ Models and Methods

Assembly of N hard/soft spheres in a box with volume V

Polydisperse spheres with pdf of diameter D $P(D) \sim D^{-3}$

Event driven molecular dynamics

To simulate hard-spheres, even-driven MD code is developed

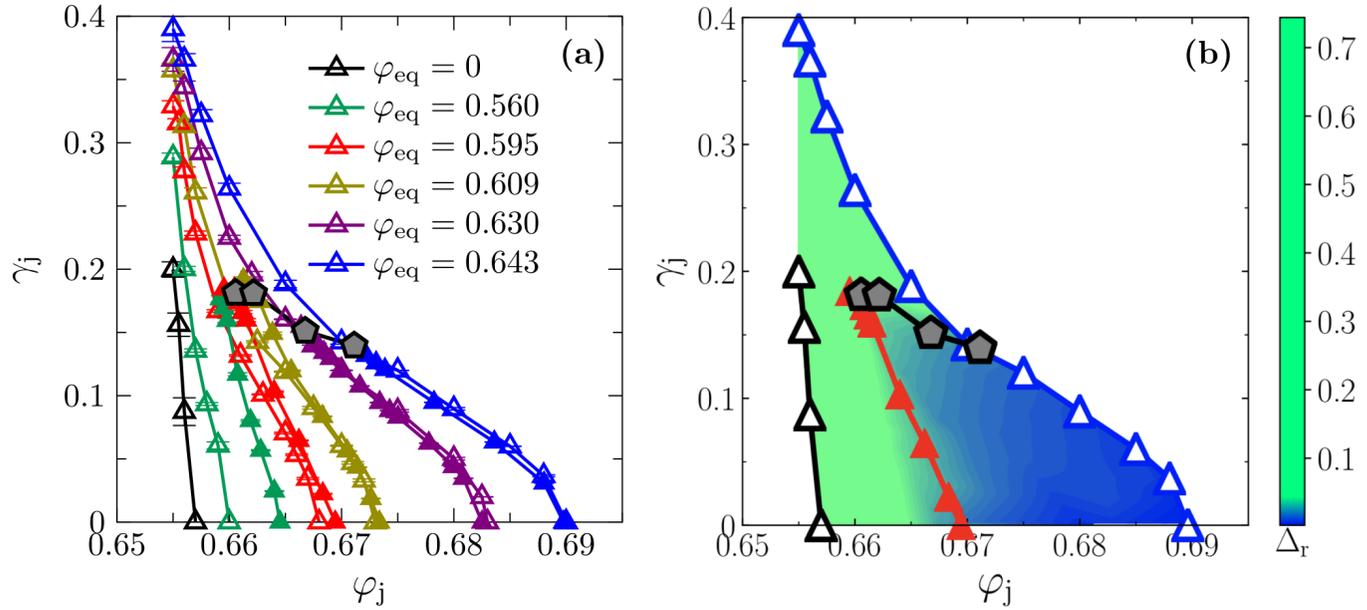
SWAP algorithm

To enhance equilibration of the initial hard-sphere configurations, the position of spheres with different radii are exchanged (GPU parallelization in progress)

FIRE algorithm

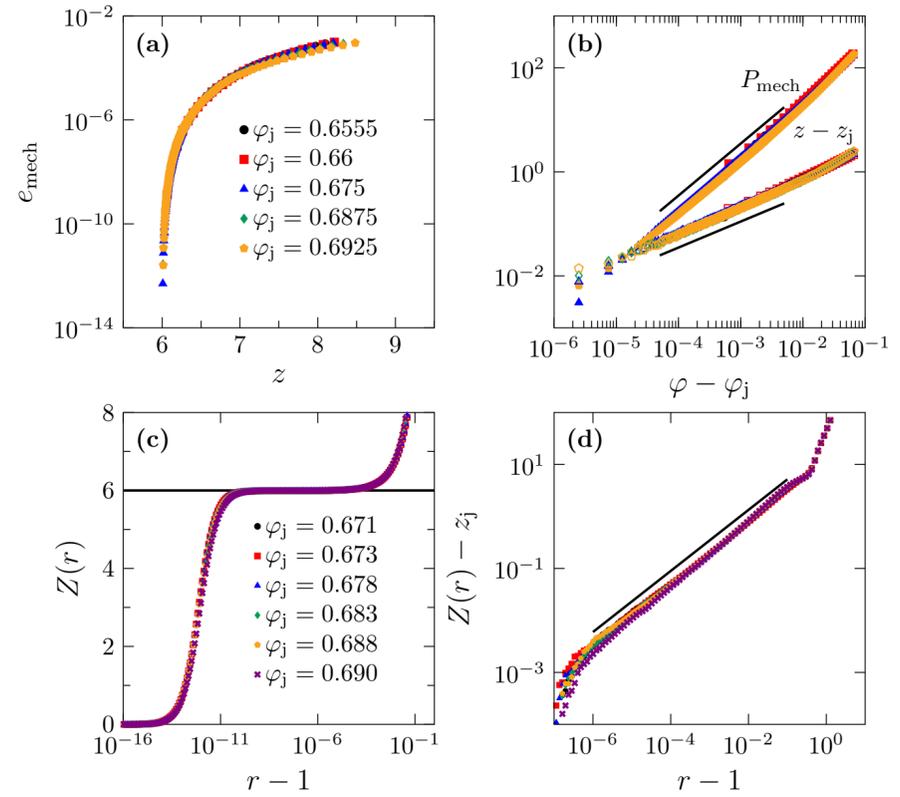
Energy minimization scheme used to remove overlaps between soft-spheres (GPU parallelization, done)

Analysis of jamming via compression/shear



(a) shear-jamming (SJ) line starting from different initial density with hard-spheres (filled symbol) and soft-spheres (empty symbols). (b) the region explored by the hard-spheres is “reversible” characterized by very small mean-squared displacement before/after cycling up to jamming from the initial states.

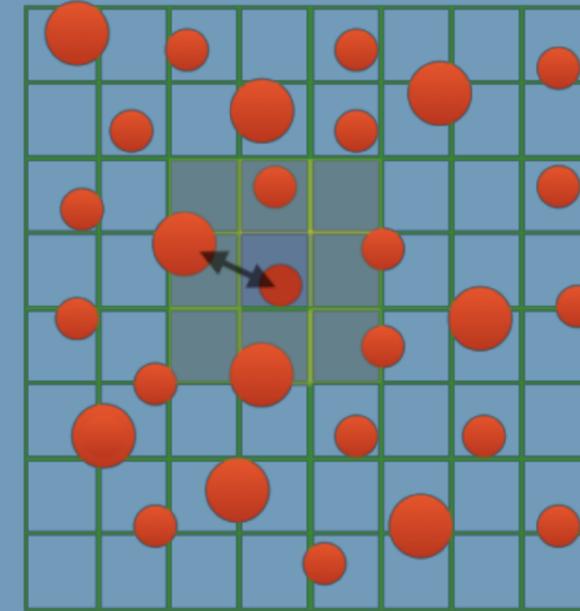
Yuliang Jin, Hajime Yoshino, ‘A Jamming Plane of sphere packings’, submitted (preprint: arXiv:2003.10814)



3 Isostaticity and universality of jamming. We show scalings (a-b) above jamming $\phi > \phi_j$ in athermal SSs, and (c-d) below jamming $\phi < \phi_j$ in thermal HSs, for $\phi_{eq} = 0.643$ and $N = 8000$. Data in (a-b) are obtained from athermal compressions of SS packings from ϕ_j to ϕ , for a few different ϕ_j along the SJ-line. (a) Energy density e_{mech} versus coordination number z . (b) Mechanical pressure P_{mech} and the excess coordination number $z - z_j$ as functions of $\phi - \phi_j$.

■ Perspective

GPU parallelization of the SWAP algorithm
(in progress)



Cell decomposition

1. Force computation can be restricted to those within the same cell or neighboring cells.
2. "Swap moves" can be vectorized/parallelized by restricting those to the particle exchange processes within the same cell or neighboring cells.

Further exploration of the non-linear rheology beyond jamming via soft-core potential model