



分子性結晶における水素ダイナミクスと同位体効果の起源解明

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Abstract

Nuclear Quantum Effect (NQE), such as zero-point vibrational energy, tunneling, and its H/D isotope effect, is quite important in various systems from small molecules to material or biochemical complex species. Especially, in the case of “**Low Barrier Hydrogen Bonding (LBHB)** systems”, NQE of proton (or deuteron) is indispensable. To elucidate such hydrogen-functional mechanism, we will develop some *ab initio* approaches for multi-component systems including both electrons and nuclei quantum-mechanically: (I) Multi-component density functional theory (**MC_DFT**) and (II) *ab initio* path integral molecular dynamics (**PIMD**) methods.

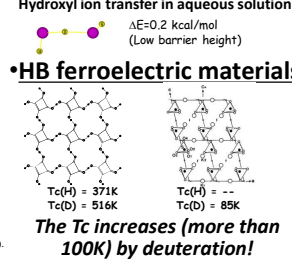
What is LBHB (Low Barrier Hydrogen Bonding) ?

•HB patterns by Jeffrey [1]

	Weak	Medium	Strong
HB Strength (kcal/mol)	< 4	4 - 15	15 - 40 (Ionic HB)
Example (X-H...A)	C-H...O	O-H...O	O-H...O ⁻ F-H-F ⁻
Geometric Isotope Effect (R _{XA})	Longer	Longer	Shorter

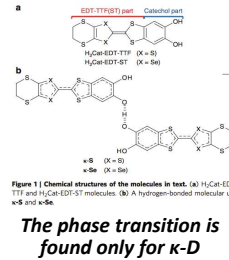
[1] G. A. Jeffrey, *An Introduction to Hydrogen Bonding*, (Oxford University Press 1997).

•Zundel structure of H₃O₂⁻

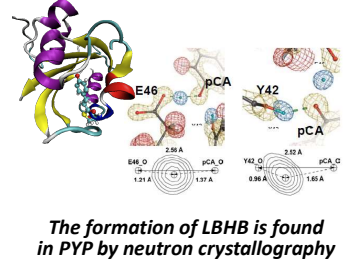


Where is LBHB?

•H₃(Cat-EDT-TTF)₂



•PYP (Photo Yellow Protein)



ab initio PIMD

-(N)-body quantum
 $\hat{H} = \sum_{i=1}^N \frac{p_i^2}{2M_i} + V(\{R_i\})$ V_0 : Potential

-(N X P)-body classical
 $Z = \text{Tr}[e^{-\beta \hat{H}}] = \text{Tr}[e^{-\beta H_{cl}}]$ ← Partition function

•Potential: *ab initio* MO

$N(-2) \times P(-8)$

Full quantum treatment !! → Path integral for nucleus
 Ab initio MO for electron

References:
 •Marx and Parrinello (1994)
 •Cheng, Barrett, and Landman (1995)
 •Schulte, Bohm, and Ramirez (1996)
 •Kitamura, Tsuneyuki, Ogitsu, and Miyake (2000)
 •M. Shiga, M. Tachikawa, and S. Miura, *J. Chem. Phys.* **115**, 9149 (2001).
 •M. Tachikawa and M. Shiga, *J. Am. Chem. Soc.* **127**, 11908 (2005).

ab initio MC_DFT

• Hamiltonian for Multi-Component system

(Electron: N, Classical nuclei: M, Quantum nuclei: L)

$$\hat{H}_{(e+p)} = \sum_{i=1}^N \frac{1}{2} \nabla_i^2 + \sum_{i=1}^N \sum_{j=1}^M \frac{1}{r_{ij}} - \sum_{i=1}^N \sum_{A=1}^M \frac{Z_A}{r_{iA}} - \sum_{a=1}^L \frac{1}{2m_a} \nabla_a^2 - \sum_{i=1}^N \sum_{a=1}^L \frac{1}{r_{ia}} + \sum_{A=1}^M \sum_{A'=1}^M \frac{Z_A Z_{A'}}{r_{AA'}} + \sum_{a=1}^L \sum_{b=1}^L \frac{1}{r_{ab}}$$

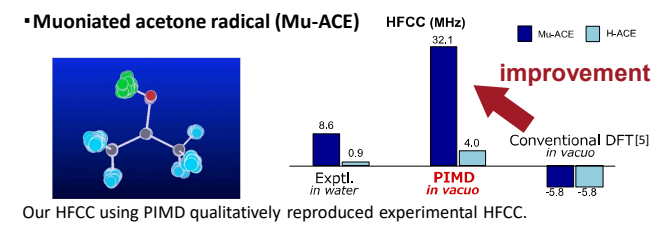
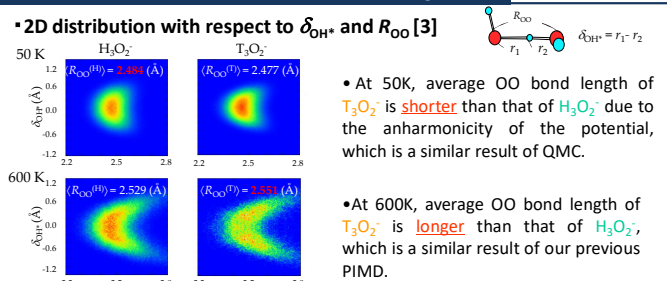
↑ Conventional DFT ↑ Quantum nuclei

• Kohn-Sham (KS) eq. for MC_DFT KS operator for MC_DFT

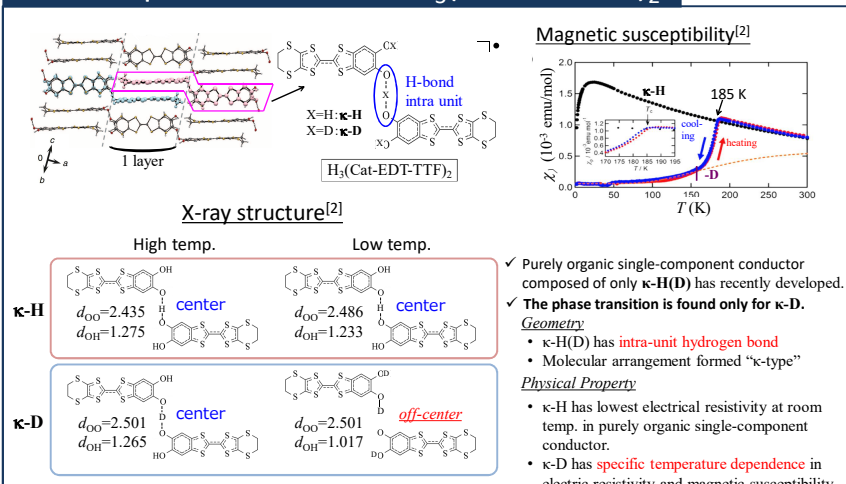
$$J_{e,p}^{(KS)} \phi_i = \epsilon_i^{e,p} \phi_i^{e,p}$$

$$J_e^{(KS)} = h_e + \sum_p \sum_c J_{pc} + V_{XC(e-e)}, \quad J_p^{(KS)} = h_p + \sum_p \sum_c J_{pc} - \sum_c J_c$$

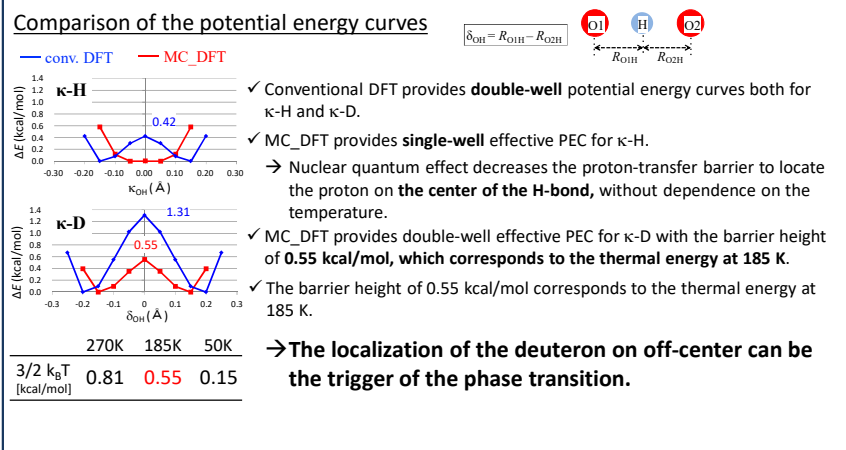
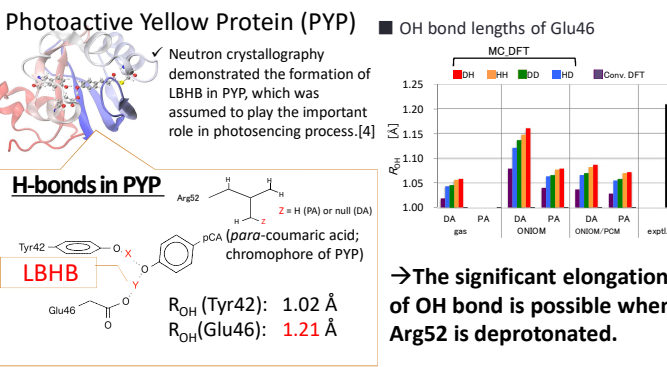
Nuclear quantum effect on H₃O₂⁻



Nuclear quantum effect on H₃(Cat-EDT-TTF)₂



Nuclear quantum effect on PYP



[1] T. Isono, H. Kamo, A. Ueda, K. Takahashi, A. Nakao, R. Kumai, H. Nakao, K. Kobayashi, Y. Murakami and H. Mori, *Nat. Commun.* **2013**, 4, 1344 [2] A. Ueda, S. Yamada, T. Isono, H. Kamo, A. Nakao, R. Kumai, H. Nakao, Y. Murakami, Y. Yamamoto, Y. Nishio and Hatsumi Mori, *J. Am. Chem. Soc.* **2014**, 136, 12184–12192 [3] T. Udagawa, M. Tachikawa, *J. Chem. Phys.*, **2006**, 125, 244105 [4] S. Yamaguchi, H. Kamikubo, et al., *Proc. Natl. Acad. Sci.*, **2009**, 106, 440 (2009). [5] R. M. Macrae et al., *Physica B*, **2003**, 326 81 (2003).